

WEEKLY TEST OYM TEST - 16 R & B
SOLUTION Date 04-08-2019

[PHYSICS]

1. Given $E = \frac{q}{4\pi\epsilon_0 x^2}$. Hence the magnitude of the electric intensity at a distance $2x$ from charge q is

$$E' = \frac{q}{4\pi\epsilon_0 (2x)^2} = \frac{q}{4\pi\epsilon_0 x^2} \times \frac{1}{4} = \frac{E}{4}$$

Therefore, the force experienced by a similar charge q at a distance $2x$ is

$$F = qE' = \frac{qE}{4}$$

Hence the correct choice is (d).

2. The system will be in equilibrium if the net force on charge q at one vertex due to charges q at the other two vertices is equal and opposite to the force due to charge Q at the centroid, i.e. (here a is the side of the triangle)

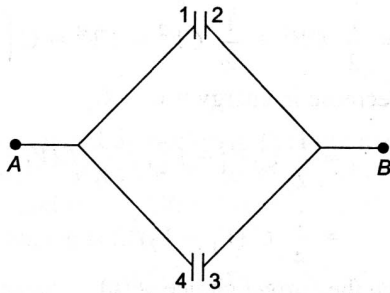
$$\frac{\sqrt{3} q^2}{4\pi\epsilon_0 a^2} = - \frac{Qq}{4\pi\epsilon_0 \left(\frac{a}{\sqrt{3}}\right)^2}$$

which gives $Q = - \frac{q}{\sqrt{3}}$. Hence the correct choice is (b).

The inner plates 2 and 3 are connected together. Hence they act as a single conductor. Since the outer plates 1 and 4 are connected together, there are effectively two capacitors (between plates 1 and 2 and plates 3 and 4) in parallel, each of capacitance $C = \epsilon_0 A/d$ as shown in Fig. 21.41. Thus the equivalent capacitance is

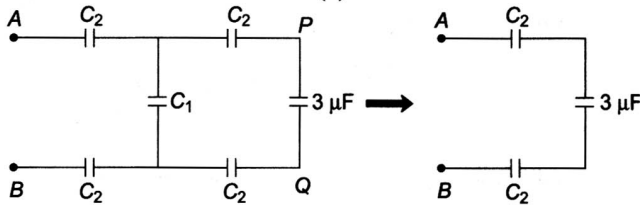
$$C' = 2C = \frac{2\epsilon_0 A}{d}, \text{ which is choice (b).}$$

3.



4.

The network reduces to that shown in Fig. 21.42. The correct choice is (a).



5. To find the force between the charged capacitor plates we will use a method called the *method of virtual displacement*. We simply equate the work ΔW required to make a small change Δd in the plate separation d to the resulting change ΔU in the stored energy, i.e.

$$\Delta W = \Delta U \quad (i)$$

If F is the magnitude of the force between the plates, then the work ΔW done to increase the plate separation by Δd is given by

$$\Delta W = F \Delta d \quad (ii)$$

Now we know that the energy U of a parallel-plate capacitor of plate area A and capacitance C is

$$U = \frac{Q^2}{2C} = \frac{Q^2 d}{2\epsilon_0 A}$$

where Q is the charge on the capacitor plates. The increase ΔU in U due to an increase Δd in d is, therefore, given by

$$\Delta U = \frac{Q^2 \Delta d}{2\epsilon_0 A} \quad (iii)$$

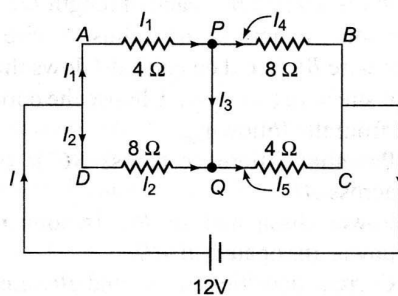
Equating Eqs. (ii) and (iii) we get

$$F = \frac{Q^2}{2\epsilon_0 A}, \text{ which is choice (c).}$$

6. Refer to Fig. 22.81. The equivalent resistance is

$$R = \frac{12 \times 12}{12 + 12} = 6 \Omega$$

$$\therefore I = \frac{12 \text{ V}}{6 \Omega} = 2 \text{ A}$$



From Kirchhoff's junction rule,

$$I_1 + I_2 = I \quad (1)$$

Using Kirchhoff's loop rule to loop $APQDA$, we have

$$4I_1 - 8I_2 = 0 \Rightarrow I_1 = 2I_2 \quad (2)$$

Equations (1) and (2) give $I_1 = \frac{4}{3}$ A and $I_2 = \frac{2}{3}$ A.

Similarly $I_4 = \frac{2}{3}$ A and $I_5 = \frac{4}{3}$ A.

Applying junction rule at P ,

$$I_1 = I_3 + I_4$$

$$\therefore I_3 = I_1 - I_4 = \frac{4}{3} - \frac{2}{3} = \frac{2}{3} \text{ A}$$

The positive sign shows that current I_3 flows from P to Q . Hence the correct choice is (c).

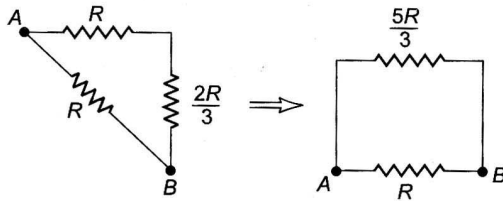
7. $I_1 = \frac{12 \text{ V}}{4\Omega} = 3 \text{ A}$

Applying Kirchhoff's loop rule to loop $ABCDE$,

$$2I_2 + E - 4I_1 = 0$$

Putting $I_1 = 3 \text{ A}$ and $I_2 = 0$, we get $E = 12 \text{ V}$

8. The circuit shown in Fig. can be redrawn as shown in Fig.



$$\therefore R_{AB} = \frac{5R}{8}, \text{ which is choice (c).}$$

9. Since the cells are in opposition, the effective emf = $6 - 2 = 4 \text{ V}$. Since the current is taken to flow from the positive to the negative terminal of the battery, a current of

$$\frac{4}{5+3} = 0.5 \text{ A}$$

flows from B to C . Hence the correct choice is (b).

10. The correct choice is (b).

11. The emfs of cells connected in reverse polarity cancel each other. Hence cells marked 2, 3 and 4 together cancel the effect of cells marked 5, 6 and 7 and the circuit reduces to that shown in Fig. 22.91. Now cells 1 and 8 are in reverse polarity. Hence the voltmeter reading = $5 - 5 = 0$ V. Hence the correct choice is (d).

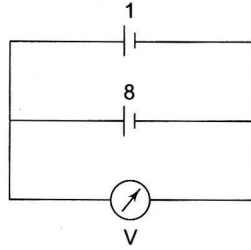


Fig. 22.91

12. The potential at Q with respect to R is 15 V and R is at 25 V higher potential than S . Thus Q is 40 V higher than S . When Q is grounded, its potential becomes zero. thus, $V_s = -40$ V. Hence the correct choice is (d).
13. The two sub circuits are closed loops. They cannot send any current through the 3Ω resistor. Hence the potential difference across the 3Ω resistor is zero, which is choice (a).

14. $R = \frac{\rho l}{\pi r^2}$. Since the two wires are made of the same material, resistivity ρ is the same for wires AB and BC . Since the wires have equal lengths, it follows that $R \propto 1/r^2$. Hence

$$\frac{R_{AB}}{R_{BC}} = \frac{1}{4}, \text{ i.e. } R_{BC} = 4R_{AB}$$

Since the current, is the same in the two wires, it follows from Ohm's law ($V = IR$) that $V_{BC} = 4 V_{AB}$. Hence choice (a) is wrong. Now power dissipated is $P = I^2 R$. Since I is the same, $P \propto R$. Hence

$$\frac{P_{BC}}{P_{AB}} = \frac{R_{AB}}{R_{BC}} = \frac{1}{4}$$

Hence choice (b) is correct. Choice (c) is wrong because current density (i.e. current per unit area) is different in wires AB and BC because their cross-sectional areas are different. The electric field in a wire is $E = V/l$. Since the two wires have the same length (l), E is proportional to potential difference (V). Since $V_{BC} = 4 V_{AB}$, $E_{BC} = 4E_{AB}$. Hence choice (d) is also incorrect.

15. Since resistances G and S are connected in parallel, the potential difference across $G =$ potential difference across $S = V$ (say). Heat dissipated in time t is

$$H = \frac{V^2 t}{R}. \text{ Hence } H \propto \frac{1}{R}$$

$$\therefore \frac{H_G}{H_S} = \frac{S}{G}$$

$$\Rightarrow \frac{2}{3} = \frac{S}{G} \Rightarrow S = \frac{2}{3} G$$

16. When the two heaters are connected in parallel, the resistance of the combination is given by

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

Now $\frac{1}{t_1} = \frac{V^2}{QR_1}$ and $\frac{1}{t_2} = \frac{V^2}{QR_2}$

Also $\frac{1}{t} = \frac{V^2}{Q} \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{1}{t_1} + \frac{1}{t_2}$

or $t = \frac{t_1 t_2}{(t_1 + t_2)}$

Hence the correct choice is (c).

17. Let I be the current in the 5Ω resistor. Then the current in the 4Ω resistor and 6Ω resistor will be $I/2$. Therefore, the rates of production of heat in the 5Ω and 4Ω resistors respectively are

$$P_1 = I^2 \times 5 \text{ and } P_2 = \left(\frac{I}{2} \right)^2 \times 4 = I^2$$

$$\therefore \frac{P_2}{P_1} = \frac{1}{5} \text{ or } P_2 = \frac{P_1}{5} = \frac{10}{5} = 2 \text{ cal s}^{-1}$$

18. Let R be the value of each resistance. The resistances of combinations I, II, III and IV are $3R$, $R/3$, $2R/3$ and $3R/2$ respectively. Now, power dissipation is inversely proportional to resistance. Hence the correct choice is (b).

19. (c) Net magnetic field at mid point P , $B = B_N + B_S$

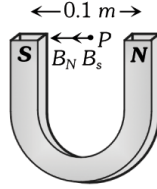
where B_N = magnetic field due to N - pole

B_S = magnetic field due to S - pole

$$B_N = B_S = \frac{\mu_0 m}{4\pi r^2}$$

$$= 10^{-7} \times \frac{0.01}{\left(\frac{0.1}{2}\right)^2} = 4 \times 10^{-7} T$$

$$\therefore B_{net} = 8 \times 10^{-7} T.$$



20. (c) For short bar magnet in tan A -position

$$\frac{\mu_0 2M}{4\pi d^3} = H \tan \theta \quad \dots(i)$$

When distance is doubled, then new deflection θ' is given by

$$\frac{\mu_0 2M}{4\pi (2d)^3} = H \tan \theta' \quad \dots(ii)$$

$$\therefore \frac{\tan \theta'}{\tan \theta} = \frac{1}{8} \Rightarrow \tan \theta' = \frac{\tan \theta}{8} = \frac{\tan 60^\circ}{8} = \frac{\sqrt{3}}{8}$$

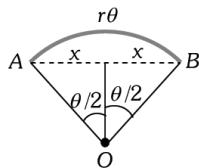
$$\Rightarrow \theta' = \tan^{-1}\left(\frac{\sqrt{3}}{8}\right)$$

21. (a) $E = nAVt = nA \frac{m}{d} t = \frac{50 \times 250 \times 10 \times 3600}{7.5 \times 10^3} = 6 \times 10^4 J$

22. (d) From figure

$$\sin \frac{\theta}{2} = \frac{x}{r}$$

$$\Rightarrow x = r \sin \frac{\theta}{2}$$



$$r\theta = l$$

$$r = \frac{l}{\theta}$$

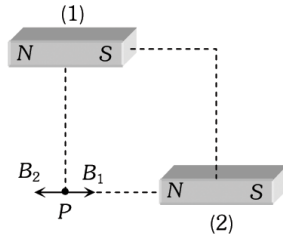
Hence new magnetic moment $M' = m(2x) = m \cdot 2r \sin \frac{\theta}{2}$

$$= m \cdot \frac{2l}{\theta} \sin \frac{\theta}{2} = \frac{2ml \sin \theta / 2}{\theta} = \frac{2M \sin(\pi/6)}{\pi/3} = \frac{3M}{\pi}$$

23. (d) Due to wood moment of inertia of the system becomes twice but there is no change in magnetic moment of the system.

$$\text{Hence by using } T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow T \propto \sqrt{I} \Rightarrow T' = \sqrt{2} T$$

24. (a) Point P lies on equatorial line of magnet (1) and axial line of magnet (2) as shown



$$B_1 = \frac{\mu_0}{4\pi} \cdot \frac{M}{d^3} = 10^{-7} \times \frac{1000}{(0.1)^3} = 0.1 T$$

$$B_2 = \frac{\mu_0}{4\pi} \cdot \frac{2M}{d^3} = 10^{-7} \times \frac{2 \times 1000}{(0.1)^3} = 0.2 T$$

$$\therefore B_{\text{net}} = B_2 - B_1 = 0.1 T$$

25. (a) Both points A and B lying on the axis of the magnet and on axial position

$$B \propto \frac{1}{d^3} \Rightarrow \frac{B_A}{B_B} = \left(\frac{d_B}{d_A}\right)^3 = \left(\frac{48}{24}\right)^3 = \frac{8}{1}$$

26. (b) $W = MB(1 - \cos \theta) = 2 \times 0.1 \times (1 - \cos 90^\circ) = 0.2 J$

27. (a) $M = mL = 4 \times 10 \times 10^{-2} = 0.4 A \times m^2$

28. (d) Magnetic potential at a distance d from the bar magnet on its axial line is given by

$$V = \frac{\mu_0}{4\pi} \cdot \frac{M}{d^2} \Rightarrow V \propto M \Rightarrow \frac{V_1}{V_2} = \frac{M_1}{M_2}$$

$$\Rightarrow \frac{V}{V_2} = \frac{M}{M/4} \Rightarrow V_2 = \frac{V}{4}$$

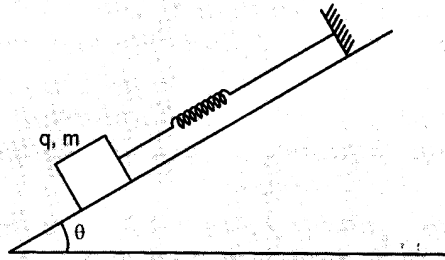
29. A

30. (d) $B_H = \sqrt{3} B_V$, also $\tan \theta = \frac{B_V}{B_H} = \frac{1}{\sqrt{3}} \Rightarrow \theta = 30^\circ$

31. (d) $R_1 < R_2$
 and $R = \frac{mv}{qB}$ of $\left(\frac{m}{q}\right)_1 < \left(\frac{m}{q}\right)_2$

32. A

33. (b) There will be no effect of magnetic force on time period because the magnetic force will be perpendicular to the inclined plane.



34. (b) If n be the number of turns and r , the radius of each turn then $n(2\pi r) = L = \text{constant}$

Also, for n turns, each turn of radius r , the torque on the total coil, when carrying the current I and placed in a magnetic field B is

$$\tau = nI (\vec{\mathbf{A}} \times \vec{\mathbf{B}}) = nI (\pi r^2) B = (\pi IB) nr^2$$

We have to maximise τ with respect to n and r subject to condition (1), treating n and r as variables substituting for nr from (1),

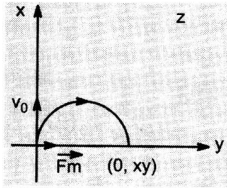
$$\tau = (\pi IB) \left(\frac{L}{2\pi}\right) r = \frac{IBL}{2} r$$

Hence, τ will be maximum when r will be maximum and the r maximum $n = 1$ (i.e.) there is only one single turn of coil.

Then $r = \frac{L}{2\pi}$

$$\tau_{\max} = \frac{IBL}{2} \cdot \frac{L}{2\pi} = \frac{L^2 IB}{4\pi}$$

$$35. \text{ (c) } y = 2r = \frac{2mv_0}{B_0q} = \frac{2v_0}{B_0\alpha}$$



Here, $\frac{q}{m} = \alpha$

36. (b)

37. C

38. (b) e.m.f. induced across the rod PQ is

$$\begin{aligned} \mathcal{E} &= \vec{\mathbf{B}} \cdot (\vec{\mathbf{1}} \times \vec{\mathbf{v}}) \\ &= Blv \sin \theta \\ &= 2 \times 2 \times 2 \times \sin 30 \\ \mathcal{E} &= 4V \end{aligned}$$

Free electrons of the rod shift towards right due to

force $q(\vec{\mathbf{v}} \times \vec{\mathbf{B}})$

Thus end P is at higher potential

or $V_P - V_Q = 4V$

39. (d) Potential difference across capacitor

$$V = Bvl = \text{constant}$$

Therefore, change stored in the capacitor is also constant. Thus, current through the capacitor is zero.

40. C

41. D

42. (c) When the rod rotates, there will be an induced current in the rod. The given situation can be treated as if a rod A of length $3l$ is rotating in clockwise direction, while another rod B of length $2l$ is rotating in the anticlockwise direction with the same angular speed ω

$$\text{As } \mathcal{E} = \frac{1}{2} B\omega l^2$$

$$\text{For A : } \mathcal{E}_A = \frac{1}{2} B\omega(3l)^2$$

$$\text{and } \mathcal{E}_B = \frac{1}{2} B(-\omega)(2l)^2$$

Resultant induced e.m.f. will be :

$$\mathcal{E} = \mathcal{E}_A + \mathcal{E}_B = \frac{1}{2} B\omega l^2(9 - 4)$$

$$\mathcal{E} = \frac{5}{2} B\omega l^2$$

43. D

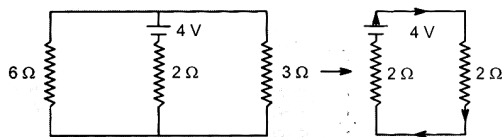
44. (c) Current in the YY' direction is from Y' to Y but the current is constant and hence the magnetic flux through the coil is constant. Therefore the current in the coil is zero.

45. (c) Motional e.m.f.

$$\mathcal{E} = Bvl$$

$$\mathcal{E} = (2)(2)(1) = 4V$$

This acts as a cell of e.m.f. $\mathcal{E} = 4V$ and internal resistance $r = 2\Omega$. The simple circuit can be drawn as follows :



∴ Current through the connector

$$I = \frac{4}{2+2} = 1A$$

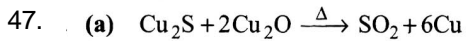
Magnetic force on connector

$$\begin{aligned} F_m &= IlB \\ &= (1)(1)(2) \\ &= 2N \quad (\text{towards left}) \end{aligned}$$

Therefore, to keep the connector moving with a constant velocity, a force of 2N will have to be applied towards right.

[CHEMISTRY]

46. Cast iron contains about 3% carbon.



48. (b) Associated colloids or micelles are formed by macro ions

49. D

50. (a)
$$E_a = \frac{2.303RT_1T_2}{T_2 - T_1} \log \frac{k_2}{k_1}$$

$$= \frac{2.303 \times 8.314 \times 293 \times 308}{15} \log 2$$

$$= 34.67 \text{ kJ mol}^{-1}.$$

51. (c)
$$t_{1/4} = \frac{2.303}{k} \log \frac{[A]_0}{3[A]_0/4}$$

$$= \frac{2.303}{k} [\log 4 - \log 3]$$

$$= \frac{2.303}{k} [0.6021 - 0.4771]$$

$$= \frac{2.303 \times 0.125}{k}$$

$$= \frac{0.2878}{k} \approx \frac{0.29}{k}$$

52. (c) When the volume of vessel is halved, the concentrations go doubled up.

$$\frac{r_{\text{new}}}{r} = \frac{k[2A][2B]^2}{k[A][B]^2} = 2 \times 2^2 = 8$$

53. (b) $r = k[A]^x$, $2r = k[4A]^x$

$$\frac{2r}{r} = \frac{k[4A]^x}{k[A]^x} \Rightarrow 4^x = 2$$

$$\Rightarrow 2^{2x} = 2^1 \Rightarrow x = \frac{1}{2}$$

$$\frac{r'}{r} = \frac{k[9A]^{\frac{1}{2}}}{k[A]^{\frac{1}{2}}} \Rightarrow \frac{r'}{r} = (9)^{\frac{1}{2}}$$

$$\Rightarrow r' = 3r$$

54. (d) w. r. t. P :

$$t_{75\%} = 2t_{50\%} \Rightarrow 1^{\text{st}} \text{ order kinetics}$$

w. r. t. Q :

Graph between concentration and time is straight line with $-ve$ slope \Rightarrow Zero order kinetics

$$\text{Overall order} = 1 + 0 = 1.$$



55. (b) $\pi = cRT$

$$\Rightarrow c = \frac{\pi}{RT} = \frac{7.8 \text{ bar}}{0.083 \text{ L bar K}^{-1} \text{ mol}^{-1} \times 310 \text{ K}} = 0.31 \text{ mol L}^{-1}$$

56. D

57. (e) Isotonic solutions have equal molarities or moles in equal volumes.

$$\frac{x}{60} (\text{urea}) = \frac{10}{342} (\text{sucrose})$$

$$x = 1.754 \text{ g in 100 mL}$$

$$\text{Wt. of urea in 1 L} = 17.54 \text{ g}$$

58. (d) For weak acid, $\alpha = \frac{i-1}{n-1}$

$$\Rightarrow 0.3 = \frac{i-1}{2-1} \Rightarrow i = 1.3$$

$$\Delta T_f = i K_f m = 1.3 \times 1.86 \times 0.1 = 0.24^\circ \text{C}$$

$$\text{Freezing point of solution} = 0 - 0.24 = -0.24^\circ \text{C}$$

59. (a) $4r = \sqrt{2} a$

$$2r = \frac{\sqrt{2}}{2} \times 408 = 288.5 \text{ pm}$$

60. (b) One Sr^{2+} creates one vacancy at site of Na^{\oplus} .
 100 moles of $\text{Na}^{\oplus} = 10^{-4}$ mole vacancies (= moles of $\text{Sr}^{2\oplus}$)

$$1 \text{ mol of Na}^{\oplus} = \frac{10^{-4}}{100} \times 6.02 \times 10^{23} = 6.02 \times 10^{17} \text{ mol}^{-1}$$

61. (b) Let $\text{Fe}^{3+} = x$ number
 so, $\text{Fe}^{2+} = 0.93 - x$
 Balancing charge, $3x + 2(0.93 - x) = 2 \Rightarrow x = 0.14$

$$\text{Fe}^{3+\%} \text{ by weight} = \frac{(0.14 \times 56) \times 100}{(0.93 \times 56) + 16} = \frac{784}{68.08} = 11.52\%$$

62. (a) One unit cell in NaCl lattice has 4 NaCl formula units.
 $4 \times 58.5 \text{ g NaCl} = 6.02 \times 10^{23} \text{ unit cells}$

$$1 \text{ g NaCl} = \frac{6.02 \times 10^{23}}{4 \times 58.5} = 2.57 \times 10^{21} \text{ unit cells}$$

63. (d) No. of equivalent of hydrogen = No. of equivalent of Al = $\frac{4.5}{9} = 0.5$
 2 gram $\text{H}_2 = 22.4 \text{ L at STP}$

$$0.5 \text{ equivalent hydrogen, i.e., } 1 \text{ g} = \frac{0.5 \times 22.4}{2} = 5.6 \text{ L}$$



79. D

80. (a) $k = Ae^{-\frac{E_a}{RT}}$

For $T_1 = T_2 = T$ and $k_1 = k_2$, we have

$$10^{15} e^{-\frac{1000}{T}} = 10^{16} e^{-\frac{2000}{T}}$$

$$e^{-\frac{1000}{T}} = 10 e^{-\frac{2000}{T}}$$

$$10 = (e^{-\frac{1000}{T}}) / (e^{-\frac{2000}{T}}) = [e]^{(-\frac{1000}{T}) - (-\frac{2000}{T})}$$

$$(e)^{2.303} = (e)^{\frac{1000}{T}} \Rightarrow T = \frac{1000}{2.303} \text{ K}$$

81.

(c) $t_{99\%} = 6.64 \times t_{1/2} = 6.64 \times 15 = 99.6 \text{ min}$

$$\begin{aligned} \text{or } t_{99\%} &= \frac{2.303}{\lambda} \log \frac{100}{100-99} = \frac{2.303 \times 15}{0.693} \times 2 \\ &= \frac{2 \times 2.303 \times 15}{0.693} = 99.69 \text{ min} \end{aligned}$$

82. D

83. (b) 10 mL of 0.5 M NaCl

$$= 10 \times 0.5 \text{ millimoles of NaCl}$$

$$= 5 \text{ millimoles of NaCl}$$

$$100 \text{ mL of total sol requires NaCl} = 5 \text{ millimoles}$$

$$1000 \text{ mL (i.e., 1 L) sol requires NaCl} = \frac{5 \times 1000}{100} = 50 \text{ millimoles}$$

84. (a) Coagulation of charged mud and sand particles by ions present in sea water, makes them settle and form the delta.

85. (a) Charged smoke particles are made to pass through charged plates (20,000 to 70,000V). Smoke particles get discharged here before coming out of the chimney.

86. C

87. C

88. (a) FeCl_2 and SnCl_2 do not react as both are reducing agents.89. (a) $K = 1 \times 10^{10}$
 $\text{F}-\underset{\text{F}}{\text{C}}\text{H}-\overset{\text{O}}{\parallel}{\text{C}}-\text{O}-\text{H}$ is the strongest among given acids and has highest degree of dissociation. So, its conductivity is the highest.

90. D